

Einführung in die Algebra
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Übungsaufgaben 2

- 1) §2, Problem 2 (Seite 7)
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Let L be a lattice. Let $x, y \in L$ be such that $x \leq y$. A **closed interval** is the set $[x, y] := \{z \in L \mid x \leq z \leq y\}$. A closed interval of a lattice is itself a lattice.

The **height** of a finite lattice is the largest n such that there is a chain of elements $x_0 < x_1 < \dots < x_n$.

Can you find a finite lattice L of height at least 3 such that every closed interval strictly smaller than L is a distributive lattice but L is not a distributive lattice?